

# Polar and Rectangular Coordinates

## Lesson 22

3.17.16-3.21.16

9.3

Converting  
Polar  
Coordinates to  
Rectangular  
Coordinates

The rectangular coordinates  $(x, y)$  of a point named by the polar coordinates  $(r, \theta)$  can be found by using the following formulas.

$$x = r \cos \theta$$

$$y = r \sin \theta$$

I try:

Find the rectangular coordinates of each point

$$P\left(5, \frac{\pi}{3}\right)$$

Identify givens	$r =$ $\theta =$
Plug into equations $x = r \cos \theta$ $y = r \sin \theta$	$x =$ $y =$

We Try:

Find the rectangular coordinates of each point

$$P(-13, -70^\circ)$$

Identify givens	$r =$ $\theta =$
Plug into equations $x = r \cos \theta$ $y = r \sin \theta$	$x =$ $y =$

You Try:

Find the rectangular coordinates of each point

$$P\left(-10, -\frac{3\pi}{2}\right)$$

<b>Converting Rectangular Coordinates to Polar Coordinates</b>	<p>The polar coordinates <math>(r, \theta)</math> of a point named by the rectangular coordinates <math>(x, y)</math> can be found by the following formulas.</p> $r = \sqrt{x^2 + y^2}$ $\theta = \text{Arctan } \frac{y}{x}, \text{ when } x > 0$ $\theta = \text{Arctan } \frac{y}{x} + \pi, \text{ when } x < 0$
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Find the polar coordinates of each point

$$R(-8, -12)$$

Identify givens	$x =$ $y =$
Plug into equations $r = \sqrt{x^2 + y^2}$ $\theta = \tan^{-1} \frac{y}{x}$	$r =$ $\theta =$

We Try:

Find the polar coordinates of each point

$R(10, -5)$

Identify givens	$x =$ $y =$
Plug into equations $r = \sqrt{x^2 + y^2}$ $\theta = \tan^{-1} \frac{y}{x}$	$r =$ $\theta =$

You Try:

Find the polar coordinates of each point

$R(3,0)$

Identify givens	$x =$ $y =$
Plug into equations $r = \sqrt{x^2 + y^2}$ $\theta = \tan^{-1} \frac{y}{x}$	$r =$ $\theta =$

## Polar and Rectangular Coordinates

Lesson 22

3.21.16

9.3

Memorize these formulas.

$$r^2 = y^2 + x^2$$

$$x = r\sin\theta$$

$$y = r\cos\theta$$

I Try:

Write the polar equation as a rectangular one.

$$r = 6\cos\theta$$

$r = 6\cos\theta$	
Multiply both sides by r	
Substitute for $r^2 = x^2 + y^2$ And $r\cos\theta = x$	

We Try:

Write the polar equation as a rectangular one.

$$r = 3\sin\theta$$

$r = 3\sin\theta$	
Multiply both sides by r	
Substitute for $r^2 = x^2 + y^2$ And $r\sin\theta = y$	

You Try:

Write the polar equation as a rectangular one.

$$r = 2$$

$r = 2$	
Multiply both sides by r	
Substitute for $r^2 = x^2 + y^2$ And $r\sin\theta = y$	

I Try:

Write the rectangular equation  $(x + 3)^2 + y^2 = 9$  as a polar equation.

$(x + 3)^2 + y^2 = 9$	
Substitute for $x = r\sin\theta$ $y = r\cos\theta$ Or $r^2 = x^2 + y^2$	
Foil	
Simplify	

We Try:

$$x = -7$$

$x = -7$	
Substitute for $x = r\sin\theta$ $y = r\cos\theta$ Or $r = x^2 + y^2$	
Simplify	

We Try:

$$x^2 - y^2 = 25$$

$x = -7$	
Substitute for $x = r\sin\theta$ $y = r\cos\theta$	

Simplify	
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You Try:

$$x^2 + (y - 3)^2 = 36$$

$x = -7$	
Substitute for $x = r\sin\theta$ $y = r\cos\theta$	
Simplify	

Exit Ticket:

1) Write the rectangular equation,  $(x - 2)^2 + y^2 = 16$  as a polar equation.

2) Write the polar equation as a rectangular one.

$$r = 3\sin\theta$$

