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Double and Half Angle Identities

Double-Angle
Identities

If θ represents the measure of an angle, then the following identities hold for all values of θ .

$$\sin 2\theta = 2 \sin \theta \cos \theta$$

$$\cos 2\theta = \cos^2 \theta - \sin^2 \theta$$

$$\cos 2\theta = 2 \cos^2 \theta - 1$$

$$\cos 2\theta = 1 - 2 \sin^2 \theta$$

$$\tan 2\theta = \frac{2 \tan \theta}{1 - \tan^2 \theta}$$

I Try:

If $\sin \theta = \frac{2}{3}$ in Q1 solve for

$\sin 2\theta$

Choose identity to use	$\sin 2\theta = 2 \sin \theta \cos \theta$
Solve for missing parts	Missing $\cos \theta$. $\cos \theta =$
Plug into formula	
Check signs	

We Try:
If $\sin\theta = \frac{2}{3}$ in Q1 solve for
 $\cos 2\theta$

Choose identity to use	
Solve for missing parts	
Plug into formula	
Check signs	

We Try:
If $\sin\theta = \frac{2}{3}$ in Q1 solve for $\tan 2\theta$

Choose identity to use	
Solve for missing parts	
Plug into formula	
Check signs	

You Try:

If $\tan\theta = \frac{4}{5}$ in Q1 solve for $\sin 2\theta$, $\cos 2\theta$, and $\tan 2\theta$,

**Half-Angle
Identities**

If α represents the measure of an angle, then the following identities hold for all values of α .

$$\sin \frac{\alpha}{2} = \pm \sqrt{\frac{1 - \cos \alpha}{2}}$$

$$\cos \frac{\alpha}{2} = \pm \sqrt{\frac{1 + \cos \alpha}{2}}$$

$$\tan \frac{\alpha}{2} = \pm \sqrt{\frac{1 - \cos \alpha}{1 + \cos \alpha}}, \cos \alpha \neq -1$$

I Try:

Use the half-angle identity to find the exact value.

$$\sin \frac{7\pi}{12}$$

Split the angle	$\sin \frac{7\pi}{12} = \sin \frac{7\pi}{6}$
Plug into formula	$\sqrt{\frac{1 - \cos \frac{7\pi}{6}}{2}}$
Simplify	$\sqrt{\frac{1 - \frac{-\sqrt{3}}{2}}{2}}$ $\sqrt{\frac{1 + \frac{\sqrt{3}}{2}}{2}}$ $\sqrt{\frac{\frac{2}{2} + \frac{\sqrt{3}}{2}}{2}}$ $\sqrt{\frac{2 + \sqrt{3}}{4}}$ $\frac{\sqrt{2 + \sqrt{3}}}{2}$

We Try:

Solve using the half angle identity $\cos 67.5$

Split the angle	
Plug into formula	
Simplify	

You Try:

$\tan 15$

Split the angle	
Plug into formula	
Simplify	

Exit Slip:

- 1) Solve using the half angle identity $\tan 15^\circ$
- 2) If $\sin \theta = \frac{2}{3}$ in Q1 solve for $\cos 2\theta$.