

Synthetic Division

Lesson 17 Part 1

10.26.15

4.3

Remainder Theorem: If a polynomial $P(x)$ is divided by $(x-r)$, the remainder is a constant $P(r)$, and $P(x) = (x - r) \cdot Q(x) + P(r)$, where $Q(x)$ is a polynomial with degree one less than the degree of $P(x)$

$$\frac{x^2 - 4}{x + 2} =$$

Factor Theorem: The binomial $x-r$ is a factor of $P(x)$ if and only if $P(r)=0$.

I do:

Divide $x^3 + 4x^2 - 5$ by $(x + 3)$

Find r in $(x - r)$	$x + 3 = x - r$ $3 = -r$ $r = -3$
Setup the coefficients. Don't forget the 0 coefficients	
Bring down first coefficient Multiply by r Add Repeat until finished	

A depressed polynomial is the resulting quotient of a division operation of a polynomial.

We Try:

$x^2 + 20x + 91$ divide by $(x + 7)$

Find r in $(x - r)$	
Setup the coefficients. Don't forget the 0 coefficients	
Bring down first coefficient Multiply by r Add Repeat until finished	

You Try with your partners on the whiteboards:
Left Talk, Right Write

$$(x^3 + x^2 - 4x - 4) \text{ divided by } (x - 2)$$

Find r in $(x - r)$	$x + 3 = x - r$ $3 = -r$ $r = -3$
Setup the coefficients. Don't forget the 0 coefficients	
Bring down first coefficient Multiply by r Add Repeat until finished	

You Try with your partners on the whiteboards:
Right Talk, Left Write

$$(2x^3 - 3x^2 + x) \text{ divided by } (x - 1)$$

Find r in $(x - r)$	$x + 3 = x - r$ $3 = -r$ $r = -3$
Setup the coefficients. Don't forget the 0 coefficients	
Bring down first coefficient Multiply by r Add Repeat until finished	

Find the remainder and state whether the binomial is a factor of the polynomial:

$$x^3 + 4x^2 - x - 4 \text{ and } (x - 2)$$

Divide by synthetic division	
If the remainder is 0, it is a factor.	